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**Third Semester B.E. Degree Examination, January 2013**  
**Field Theory**

Time: 3 hrs.

Max. Marks:100

**Note:** Answer any FIVE full questions, selecting atleast TWO questions from each part.

**PART - A**

- 1 a. Define the following : i) Coulomb's law    ii) Electric field intensity    iii) Gauss law. (06 Marks)
- b. State the prove divergence theorem. (06 Marks)
- c. Let  $\vec{D} = 5r^2 \mathbf{a}_r \text{ mc / mt}^2$  for  $r < 0.08\text{mt}$   
and  $\vec{D} = \frac{0.1}{r^2} \mathbf{a}_r \text{ mc/mt}^2$  for  $r > 0.08 \text{ mt}$ . Find  $\rho_v$  for i)  $r = 0.06 \text{ mt}$     ii)  $r = 0.1 \text{ mt}$ . (08 Marks)
- 2 a. An electric potential is given by  $V = \frac{60 \sin \theta}{r^2}$ . Find  $v$  and  $\vec{E}$  at  $(3, 60^\circ, 25^\circ)$ . (08 Marks)
- b. Derive the integral and point form of continuity equation. (06 Marks)
- c. Derive the boundary conditions for perfect dielectric materials of permittivities  $\epsilon_1$  and  $\epsilon_2$ . (06 Marks)
- 3 a. Obtain Poisson's and Laplace's equations from Maxwell's first equation. (06 Marks)
- b. Verify that the potential field given below satisfy Laplace's equation.  
 $V = 2x^2 - 3y^2 + z^2$ . (06 Marks)
- c. Derive the expression for capacitance of a co – axial cable using Laplace's equation. (08 Marks)
- 4 a. State and explain Biot – Savart law. Using this, find the magnetic flux density at the centre of a circular loop of radius 'a' mt. (08 Marks)
- b. Magnetic field intensity in free space is  $\vec{H} = 10\rho^2 \mathbf{a}_\phi \text{ A/mt}$ . Determine i)  $\vec{J}$     ii) Integrate over the circular surface  $\rho = 1\text{mt}$  all  $\phi$  and  $Z = 0$ . (06 Marks)
- c. Explain scalar and vector magnetic potentials. (06 Marks)

**PART - B**

- 5 a. Derive the equation for magnetic force between two differential current elements. (06 Marks)
- b. Given the ferrite material which is to be operating in a linear mode with  $\vec{B} = 0.05\text{T}$  and  $\mu_R = 50$ . Calculate the values for  $\chi_m$ ,  $\vec{M}$  and  $\vec{H}$ . (06 Marks)
- c. Define self inductance. Find the same of a Solenoid with air core has 200 turns and a length of 60cm core with radius 3cm. Derive the formula used. (08 Marks)
- 6 a. Derive the Maxwell's equation in point form as derived from Faraday's law. (06 Marks)
- b. Determine the frequency at which conduction current density and displacement current density are equal in a medium with  $\sigma = 2 \times 10^{-4} \text{ S/mt}$  and  $\epsilon_r = 81$ . (06 Marks)
- c. List the Maxwell's equation in differential and integral form as applied to time – varying fields. (08 Marks)

- 7 a. Discuss the uniform plane wave propagation in a good conducting medium. **(06 Marks)**
- b. A 9375 MHz uniform plane wave is propagating in polystyrene ( $\mu_r = 1$ ,  $\epsilon_r = 2.56$ ). If the amplitude of electric field intensity is 20V/m and the material is assumed to be lossless. Find i) Phase constant ii) Wavelength iii) Velocity of propagation iv) Intrinsic impedance v) Magnetic field intensity. **(10 Marks)**
- c. State and explain Poynting theorem. **(04 Marks)**
- 8 a. Define Standing wave ratio (SWR). Find the value of SWR when reflection co-efficient ( $\Gamma$ ) =  $\pm \frac{1}{2}$ . **(04 Marks)**
- b. Derive the expressions for transmission co – efficient and reflection co – efficient. **(08 Marks)**
- c. Determine the reflection co – efficient and transmission co – efficient for a wave traveling in air and incident on a dielectric medium with  $\mu = \mu_0$  and  $\epsilon_r = 4$ . Also find out average incident, reflected and transmitted powers. Show that average power is conserved. **(08 Marks)**

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